

# On the role of contextual information for privacy attacks and classification

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## Abstract

*Many papers and articles attempt to define or even quantify privacy, typically with a major focus on anonymity. A related research exercise in the area of evidence-based trust models for ubiquitous computing environments has given us an impulse to take a closer look at the definition(s) of privacy in the Common Criteria, which we then transcribed in a bit more formal manner. This led us to a further review of unlinkability, and revision of another semi-formal model allowing for expression of anonymity and unlinkability – the Freiburg Privacy Diamond. We propose new means of describing (obviously only observable) characteristics of a system to reflect the role of contexts for profiling – and linking – users with actions in a system. We believe this approach should allow for evaluating privacy in large data sets.*

## 1. Introduction

This paper outlines the development of our appreciation of privacy concepts that started with a research exercise on data mining in evidential data for evidence-based reputation systems. The novel idea of evidence-based reputation (or trust) systems is that such systems do not rely on an objective knowledge of user identity [1, 2, 11]. One has instead to consider possible privacy infringements based on the use of data (evidence) about previous behaviour of entities in the systems. We provide a brief introduction to evidence-based trust/reputation systems, as well as to the privacy issues, addressing the common problem of many papers that narrow the considerations of privacy to anonymity only.

The paper is structured in the following way – remaining parts of this introductory section provide a brief overview of issues related to evidence-based systems, Common Cri-

teria and Freiburg Privacy Diamond models, motivation for our research, and a simple example used to illustrate the use of privacy models. Section two then presents some of the Common Criteria concepts used in the following discussions, and also outlines the Common Criteria approach to privacy issues (families), together with a discussion of unlinkability – the most complex property/quality of privacy. The third section presents the Freiburg Privacy Diamond – a semi-formal model allowing for expression of anonymity and unlinkability, focussing on the mobile environment. Section four then examines the role of contexts in these two approaches to modelling privacy. This leads to the fifth section that proposes using contextual information to model systems for privacy evaluations, and presents non-existential definitions of the four Common Criteria privacy concepts. Section six concludes with an outline of related ideas and open issues.

### 1.1 Evidence-based trust/reputation

Evidence-based systems work basically with two sets of evidence (data describing interaction outcomes). The primary set contains evidence that is delivered (or selected from locally stored data) according to a given request content. That data is used for reputation evaluation to grant/reject access requests. Data in this first set may contain information from third parties representing evidence about behaviour collected by other nodes – recommenders.

The secondary set comprises data relevant to a local system. That data is used for self-assessment of the local system security in various contexts (it may be a non-deterministic process in a certain sense). This set may be also referenced as derived or secondary data. Note that there may be an intersection between the two evidence sets with implications to privacy issues that we are investigating in related projects [4, 5].

The approach of reputation systems is rather probabilis-

tic and this feature directly implies properties of security mechanisms that may be defined on top of such systems. The essential problem arises with recommendations that may be artificially created by distributed types of attacks (Sybil attack [7]) based on large number of nodes created just to gather enough evidence and achieve maximum reputation that would allow them to launch their attack(s).

## 1.2 A note on the Common Criteria and Freiburg Privacy Diamond models

This paper proposes formal definitions of existing Common Criteria concepts/areas of privacy and compares them with the Freiburg Privacy Diamond model (FPD) [18]. Recent research in anonymity systems [6, 10, 15] demonstrates that it is usually unfeasible to provide perfect anonymity and that implementations of privacy enhancing systems may provide only a certain level of privacy (anonymity, pseudonymity). This lead to definitions of several metrics that can quantify level of privacy achievable in a system, most often a (remailing) mix.

The Common Criteria class Privacy deals with aspects of privacy as outlined in their four families. Three of these families have a similar grounding with respect to entities (i.e., users or processes) whose privacy might be in danger. They are vulnerable to varying threats, which make them distinct from each other. These families are Unobservability, Anonymity, and Unlinkability. The fourth family – Pseudonymity – addresses somewhat different kind of threats.

## 1.3 Motivation

While working on related issues [5], we became aware of the need to define the Common Criteria concepts (called families) dealing with privacy in a bit more precise fashion. As we were examining definitions of privacy concepts/families as stated in Common Criteria two negative facts emerged. First, the definitions are given in an existential manner, and secondly, not all aspects of user interactions relevant to privacy are covered. Both issues come from research carried out in the areas of side-channel analysis and security of system implementations, showing that it is not sufficient to take into account only the idealised principals and messages. It is also very important to consider the context, in/with which the interactions are undertaken. Information like physical and virtual (IP, MAC addresses) positions of users and computers, time, type of service invoked, size of messages, etc. allow to profile typical user behaviour and successfully deteriorate privacy of users in information systems.

We propose to introduce context information (side/covert channels, like physical and virtual location of users and

computers, time, type of service invoked, size of messages, etc.) into the CC model and compare it with the FPD model that reflects only one very specific context information – location.

Our objectives for starting this work are as follows. Firstly, we want to provide a model that allows one to cover as many aspects of user interactions as is beneficial for improving quantification/measurement for different aspects of privacy; this model shall definitely provide for better reasoning/evaluation of privacy than Common Criteria and Freiburg Privacy Diamond models do. Secondly, and in a close relation to the first objective, we want to illustrate the deficiency of the Common Criteria treatment of privacy, and to provide a foundation that would assist in improving this treatment. Thirdly, with a long-term perspective, we aim to provide basis for partly or fully automated evaluation/measurement of privacy.

This paper does not address all aspects of data collection for privacy models, and neither does it suggest any means for improving the level of privacy protection.

## 1.4 A simple example

Let us present a trivial example that we use later in this paper to compare the formal models for privacy. The attacker attempts to determine which payment cards are used by a certain person with a particular card – she is interested in linking together all the cards of this person (identification of the particular person is not part of the attacker’s goal at the moment). We assume the attacker is able to collect till receipts of shoppers from the same house or the same company. For this subset of supermarket clients we then do not mind a given receipt to show only a part of the payment card number.

There are three payment cards (with numbers 11, 21, 25) used for three actual shoppings (visits of the supermarket resulting in payments –  $A$ ,  $B$ ,  $C$ ), and there is also a set of typical baskets/shopping lists ( $l$ ,  $m$ ) in our simplistic example.

The attacker has a precise (100%) knowledge about connections between payment cards and shoppings, and an imprecise knowledge about classification of individual shoppings into typical “consumer group” baskets. This classification to “typical baskets” is usually done with some kind of a data-mining algorithm over actual shopping lists. Note that one could obviously achieve perfect knowledge should loyalty cards be used (and their numbers on the receipts), introduction of this has no qualitative impact to this example illustration in our model.

With just changing semantics, we may define a very similar example based on users of chat services connecting from a given Internet cafe. The categories would then be chat-room pseudonyms, chat sessions, and classifica-

tion into groups based on interest (content) and/or language, with the attacker’s goal of identifying pseudonyms used by one user in different chat sessions.

## 2. Privacy in the Common Criteria

### 2.1. The starting point – model

Since some of the discussions and proposals in this paper are based on the Common Criteria concepts, let us briefly present the related information. Relevant Common Criteria notions and concepts are as follows [17]:

**Target of Evaluation (TOE)** – An IT product or system and its associated administrator and user guidance documentation that is the subject of an evaluation.

**TOE Security Functions (TSF)** – A set consisting of all hardware, software, and firmware of the TOE that must be relied upon for the correct enforcement of the TOE security policy.

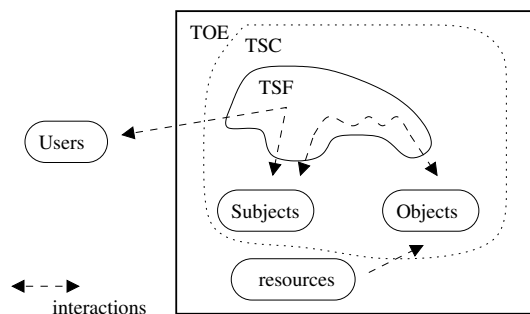
**TSF Scope of Control (TSC)** – The set of interactions that can occur with or within a TOE and are subject to the rules of the TOE security policy.

**Subject** – An entity within the TSC that causes operations to be performed.

**Assets** – Information or resources to be protected by the countermeasures of a TOE.

**Object** – An entity within the TSC that contains or receives information and upon which subjects perform operations.

**User** – Any entity (human user or external IT entity) outside the TOE that interacts with the TOE.



**Figure 1. Common Criteria model.**

We can see (fig. 1) that user does not access objects directly but through subjects – internal representation of herself inside TOE/TSC. This indirection is exploited for definition of pseudonymity as we will see later. Objects represent not only information but also services mediating access

to TOE’s resources. This abstract model does not directly cover communication like in (remailer) mixes as it explicitly describes only relations between users/subjects and resources of target information system. However, it is not difficult to extend the proposed formal definitions of major privacy concepts based on this model for communication models.

### 2.2 Privacy in the Common Criteria

**Unobservability** : *This family ensures that a user may use a resource or service without others, especially third parties, being able to observe that the resource or service is being used.* The protected asset in this case can be information about other users’ communications, about access to and use of a certain resource or service, etc. Several countries, e.g. Germany, consider the assurance of communication unobservability as an essential part of the protection of constitutional rights. Threats of malicious observations (e.g., through Trojan Horses) and traffic analysis (by others than communicating parties) are best-known examples.

**Anonymity** : *This family ensures that a user may use a resource or service without disclosing the user identity. The requirements for Anonymity provide protection of the user identity. Anonymity is not intended to protect the subject identity.* Although it may be surprising to find a service of this nature in a Trusted Computing Environment, possible applications include enquiries of a confidential nature to public databases, etc. A protected asset is usually the identity of the requesting entity, but can also include information on the kind of requested operation (and/or information) and aspects such as time and mode of use. The relevant threats are: disclosure of identity or leakage of information leading to disclosure of identity – often described as “usage profiling”.

**Unlinkability** : *This family ensures that a user may make multiple uses of resources or services without others being able to link these uses together.* The protected assets are of the same as in Anonymity. Relevant threats can also be classed as “usage profiling”.

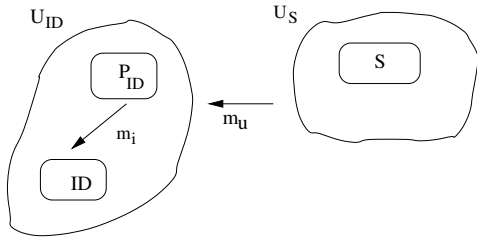
**Pseudonymity** : *This family ensures that a user may use a resource or service without disclosing its user identity, but can still be accountable for that use.* Possible applications are usage and charging for phone services without disclosing identity, “anonymous” use of an electronic payment, etc. In addition to the Anonymity services, Pseudonymity provides methods for authorisation without identification (at all or directly to the resource or service provider).

### 2.3. Privacy families revisited

Common Criteria privacy families are defined in an existential manner and any formal definition of them has to tackle a number of ambiguities. It is unrealistic to assume perfect/absolute privacy as demonstrated by several anonymity metrics, based on anonymity sets (number of users able to use a given resource/service in a given context) [12] or entropy assigned to a projection between service and user/subject identities (uncertainty about using a service) [15].

Can we introduce more formal definition of privacy notions and use them to define mutual relations? It is not easy, but the prospects of getting a clearer picture of mutual relations between different privacy aspects/qualities are encouraging.

Our proposal for the CC model privacy formalisation is based on the following graphical representation (fig. 2). The set  $S$  represents observations of uses of services or resources,  $P_{ID}$  is equivalent of subjects and  $ID$  stands for users as defined in the CC. Sets  $U_S$  and  $U_{ID}$  are sets of all possible service use observations and identities, respectively – not only those relevant for a given system. By stating *with probability not significantly greater than* in the following definitions, we mean negligible difference (lower than  $\varepsilon$ ) from a specified value [3]. Let  $\mathcal{A}$  be any attacker with unbounded computing power.



**Figure 2. Schematics for the CC view of privacy.**

Our formal transcription of existential definitions of CC privacy families is as follows.

**Unobservability** – there is a space of encodings ( $U_S$ ) from which some elements are defined to encode use of service/resource ( $S$ ). However,  $\mathcal{A}$  is not able to determine  $\forall s \in S$  with a probability significantly greater than  $1/2$  whether a particular  $s \in S$  or  $s \in (U_S - S)$ .

**Anonymity** – there is a probability mapping  $m_u : S \rightarrow U_{ID}$ . When

1.  $\mathcal{A}$  knows the set  $ID$  – then  $\forall s \in S, u_{ID} \in ID$ ,

she can only find  $m_u(s) = u_{ID}$  with a probability not significantly greater than  $1/|ID|$ .

2.  $\mathcal{A}$  does not know anything about  $ID$  (particular elements or size) – then for  $\forall u_{ID} \in U_{ID}$ , she cannot even guess whether  $u_{ID} \in ID$  with a probability significantly greater than  $1/2$ . (The probability of finding  $m_u(s) = u_{ID}$  would not be significantly greater than 0.)

**Unlinkability** – let us assume there is a function  $\delta : m \times S \times S \rightarrow [no, yes]$ . This function determines whether two service uses were invoked by the same  $u_{ID} \in U_{ID}$  or not. Parameter  $m$  stands for a function that maps service uses ( $S$ ) into a set of identities  $U_{ID}$  (e.g.,  $m_u$  from fig. 2).

It is infeasible for  $\mathcal{A}$  with any  $\delta$  and any  $s_1, s_2 \in S$ ,  $s_1 \neq s_2$  to determine whether  $m(s_1) = m(s_2)$  with a probability significantly greater than  $1/2$ .

**Pseudonymity** – there exists and is known to  $\mathcal{A}$  an unambiguous mapping  $m_u(s) = u$ ,  $\forall s \in S$ ,  $u \in P_{ID}$ . There also exists a mapping  $m_i(u) = u_{ID}$ ,  $\forall u \in P_{ID}$ ,  $u_{ID} \in ID$ , but is subject to strict conditions and not known to  $\mathcal{A}$ . When  $\mathcal{A}$

1. knows  $ID$ , she cannot determine correct  $u_{ID}$  with a probability significantly greater than  $1/|ID|$ ;
2. does not know  $ID$ , she can only guess with a probability not significantly greater than  $1/2$  whether  $u_{ID} \in ID$ .

These existential expressions can then be easily turned into probabilistic ones that allow for expressing different qualitative levels of all these privacy concepts/families. This can be done simply by changing the “not significantly greater than” expression to “not greater than  $\Delta$ ”, where  $\Delta$  is the given probability threshold.

### 2.4 The Unlinkables

Unlinkability cannot be satisfied without other privacy families. It is now understood [13, 14] that the Common Criteria definition of unlinkability is not supporting some aspects of unlinkability in real systems, and a Common Criteria modification proposal in this manner is currently submitted. We point the reader to the fact that when pseudonymity is flawed, an attacker may obtain the ID of an actual user. The same holds when anonymity is breached.

Moreover, we are convinced that unlinkability may be a property of other privacy families. This comes straight from the formal unlinkability definition as stated above, where mapping  $m$  is the link binding the families together. Unlinkability should ensure that the particular family (or rather

its implementation) does not contain side-channels (context information) that could be exploited by an attacker. We have found, in this context, two other meanings for unlinkability during our analysis. The first meaning is expressed in the following definition of unlinkable pseudonymity. It says that when a user employs two different pseudonyms, any  $\mathcal{A}$  is not able to connect these two pseudonyms together.

**Unlinkable pseudonymity** – As for the definition of pseudonymity above in part 2.3, and also for any  $s_1, s_2 \in S$ , where  $s_1 \neq s_2, m_u(s_1) = u_1, m_u(s_2) = u_2$  (where  $u_1, u_2 \in P_{ID}$ )

1. If  $\mathcal{A}$  knows  $ID$  – she cannot find (with a probability significantly greater than  $1/|ID|$ ), whether  $m_i(u_1) = m_i(u_2)$ , or
2.  $\mathcal{A}$  does not know  $ID$  – she cannot guess with a probability significantly greater than  $1/4$  whether  $\frac{m_i(u_1) \times m_i(u_2)}{ID \times ID}, \frac{ID \times ID}{ID \times ID}, \frac{ID \times ID}{ID \times ID}$ , respectively. ( $\overline{ID} = U_{ID} - ID$ )

The second semantics is built on the assumption that knowledge of several pieces of mutually related information is much more powerful than knowledge of just one piece of such information. When compared with the previous definition of unlinkable pseudonymity, the definition is now concerned with a property ensuring that there is no increase in the probability of correct identification of a given user when more information is available. The same reasoning lies behind the following definition of unlinkable anonymity.

**Unlinkable anonymity** – As for the definition of anonymity above in part 2.3, and

1. if  $\mathcal{A}$  knows  $ID$  – she cannot find with a probability significantly greater than  $1/|ID|$  such  $s_1, s_2 \in S$ , where  $s_1 \neq s_2, m_u(s_1) = m_u(s_2)$ .
2.  $\mathcal{A}$  does not know  $ID$  – with a probability not significantly greater than  $1/4$  whether  $\frac{m_u(s_1) \times m_u(s_2)}{ID \times ID}, \frac{ID \times ID}{ID \times ID}, \frac{ID \times ID}{ID \times ID}$ , respectively.

We can apply profiling when unlinkability is breached. Basically, unlinkability should ensure that the particular family (or its implementation) does not contain side-channels that could be used when several service invocations appear.

**The example:** The figure 3 depicts how CC models our example from part 1.4. It is obvious that there is no information about the context information for the basket (chat) contents. This implies that an attacker will not find any link between payment cards (pseudonyms) using this model, even

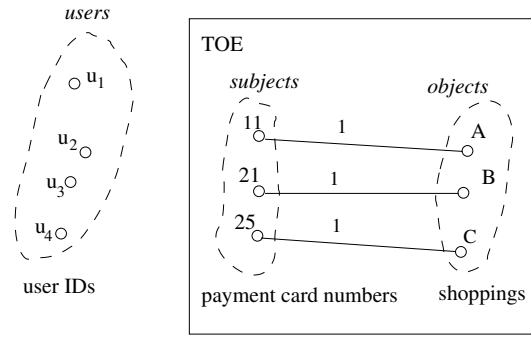


Figure 3. The example in CC model.

though the link/connection exists. This shows that CC simply do not address contextual information.

### 3. Freiburg Privacy Diamond

FPD is a semiformal anonymity (and partly also unlinkability) model by A. Zugenmaier et al. [18, 19]. The model originated from their research in the area of security in mobile environments. The model is graphically represented as a diamond with vertices User, Action, Device (alternatives for CC’s user, service, and subject), and Location (fig. 4). The main reason for introducing *location* as a category here is probably due to the overall focus of this model on mobile computing.

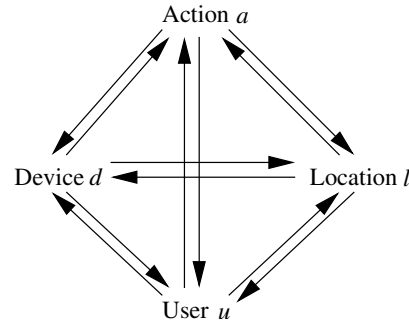


Figure 4. Freiburg privacy diamond.

Anonymity of a user  $u$  performing an action  $a$  is breached when there exists a connection between  $a$  and  $u$ . This may be achieved through any path in the diamond model. Let us recap basic definitions of the FPD model:

1. Any element  $x$  has got a type  $type(x) \in \{User, Action, Device, Location\}$ . Any two elements, such as  $x, y \in \{e | type(e) = User \vee Action \vee Device \vee Location\}, type(x) \neq type(y)$  are in a relation  $R$  if the attacker has evidence connecting  $x$  and  $y$ .

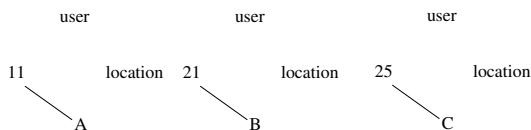
2. An action is anonymous if  $U_R = \{u \mid type(u) = User \wedge (u, a) \in R\}$  is either empty or  $|U_R| > t > 1$ , where  $t$  is an anonymity threshold defining minimum acceptable size of anonymity set.
3. There is the transitivity rule saying that if  $(x, y) \in R$  and  $(y, z) \in R$ , and  $type(x) \neq type(z)$ , then  $x, z \in R$ .
4. The union of all initial relations known to an attacker  $\mathcal{A}$  defines his initial view  $View_{\mathcal{A}}$ .
5. The transitive closure  $\overline{View_{\mathcal{A}}}$  of  $View_{\mathcal{A}}$  defines all the information an attacker  $\mathcal{A}$  may infer from her initial view.

The book [18] also introduces three types of attacks with context information.

- **Recognition attack** –  $\mathcal{A}$  realises that several users ( $x_i, type(x_i) = User$ ) are in fact a single user.
- **Linking attack** –  $(x, y) \in R$  and  $(z, y) \in R$  are in the  $\overline{View_{\mathcal{A}}}$ . When  $\mathcal{A}$  is able to find just one pair  $(y, x_i) \in R$  then she will know that  $x_i = x$  and  $(z, x) \in R$ .
- **Intersection attack** –  $\mathcal{A}$  knows anonymity sets for several actions. When she knows that a certain user is in all anonymity sets, she can apply intersections to reduce size of anonymity set and eventually identify the user.

Finally, the model assigns probabilities to edges in order to express attacker’s certainty about existence of particular relations with some simple rules how to derive certainty for transitive relations.

**The example:** When attempting to model the example scenario (see part 1.4) in the FPD model, the attacker ends up with three diamonds for each service use (see fig 5). Here *user* and *location* represent domains with no particular values as there is no such information available. The attacker cannot find any intersection of the three diamonds – i.e., there is no attack as defined by the FPD model theory. This is obvious since the FPD model does not cover any other contextual information, only location and device.



**Figure 5. The example with in FPD model.**

## 4. Contexts in the two models

Contexts and their roles are not reflected in the CC model. Considering fig. 2, we see that the two vectors in question ( $m_i, m_u$ ) are bound together through a pseudonym – subject in the CC language. Contexts may be assigned to any element of the model. *ID* represents physical entities and we may know their mobile phone locations, addresses, patterns of network usage, etc.  $P_{ID}$  – virtual IDs – can be characterised by previous transactions and possibly virtual locations (a virtual location may be in some cases very effectively mapped on a physical location). Elements of  $S$  may be further characterised by type, provider, etc.

The edges between sets (their elements) represent sessions taking place in the system. The information we may gather about them are highly dependent on actual implementation of the system and may comprise contextual information such as time, length, routing path, content, etc.

### 4.1 Contexts in FPD

The FPD model only briefly mentions context information but does not introduce any definition of it. The attacks based on context information do not say how to perform them but only defines changes in  $\overline{View_{\mathcal{A}}}$  when an attack is completed.

Since the FPD model newly addressed the mobile computing environment, as opposed to the old-fashioned “static” environment, location had a very prominent role, as did the device to some extent. We have decided to treat these as “ordinary” context information, i.e. as any other additional information about the system that can link a user and an action (or more precisely, their identifiers).

## 5 Context revisited – basics of the PATS (Privacy Across-The-Street<sup>1</sup>) model

We propose the following approach, inspired by the way location and device (descriptors) are represented in FPD.

We suggest all context information available to an attacker to be represented as vertices in a graph, where edges are weighed with the probability of the two incident vertices (contextual information, user and service IDs) to be related/connected. Those connections may be between any two vertices, and a path connecting a user ID and a service ID with a certain probability value of the path suggests a link between the service use and the user ID exists.

The graph reflects all knowledge of an attacker at a given time. Attackers with different knowledge will build different graphs for a system as will likely do the same attacker over some time.

<sup>1</sup>Authors of this proposal work for different institutions located across the street.

What is not clear to us at the moment is the question whether pseudonyms should be treated differently from other contexts or not. Clearly they are more important in the model since their connection to users and actions defines level of pseudonymity achieved in the system. Yet at the moment we suggest all vertices to be treated equally, although we suspect that some of them might be more equal than others. :-)

### 5.1 Outline of the graph model

We denote the set of all vertices by  $V$ , the set of all identifiers of service instances by  $S$ , and the set of all user IDs by  $ID$ . There are no edges between any pair of elements of  $ID$ , only indirect paths through a linking context, and the same applies to elements of  $S$ . There is also a function  $W_{max}$  calculating overall probability weight for a path in the graph, and therefore also a way to determine the highest value  $W_{max}(v_a, v_b)$  for a path between  $v_a$  and  $v_b$ . The value of any path is calculated as a multiplication of the weights ( $w$ ) of all its individual edges, e.g. for the path  $P = v_1, v_2, \dots, v_i$  of  $i$  vertices of the graph, the value of the path  $P$  is  $W(v_1, v_i) = w(v_1, v_2) \times w(v_2, v_3) \times \dots \times w(v_{i-1}, v_i)$ .

**Unobservability** (of service  $s_i$ ) – a graph that  $\mathcal{A}$  can build after observing a system at a given time does not include  $s_i$  at all.

**Unlinkability** (between two nodes  $v_1, v_2$ , at the level  $\Delta$ ) – a graph that  $\mathcal{A}$  can build when observing the system at a given time has no path connecting  $v_1$  with  $v_2$  with the overall probability greater than  $\Delta$ , i.e. provides  $W(v_1, v_2) \leq \frac{1}{|V_1 \cdot V_2|} + \Delta$ , where  $v_1 \in V_1$  and  $v_2 \in V_2$ .

**Anonymity** (of a user  $u_{ID} \in ID$ , at the level  $\Delta$ ) – then  $\forall v \in V$ , when  $\mathcal{A}$

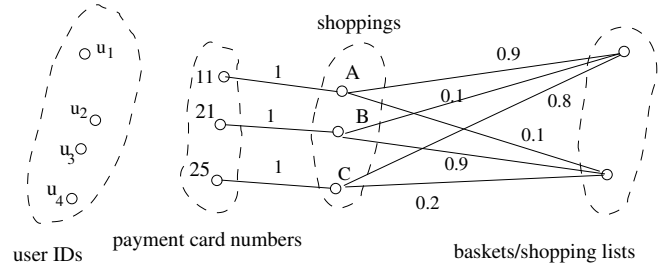
1. knows the set  $ID$ , she can only find a path from  $v$  to  $u_{ID}$  with the weight not greater than  $1/|ID| + \Delta$  such that  $W_{max}(v, u_{ID}) \leq 1/|ID| + \Delta$ ;
2. does not know anything about  $ID$  (particular elements or size), she can only find a path from  $v$  to  $u_{ID}$  with the weight not greater than  $\Delta$ , i.e.  $W_{max}(v, u_{ID}) \leq \Delta$ .

**Pseudonymity** (of a subject/pseudonym  $u \in P_{ID}$ , at the level  $\Delta$ ) – there exists a path known to  $\mathcal{A}$  from any  $s \in S$  to  $u$  with a satisfactory value of  $W_{max}(s, u)$ , but for  $\mathcal{A}$  there is no knowledge of an edge from  $u$  to any  $u_{ID} \in ID$  such that when  $\mathcal{A}$

1. knows  $ID$ , the path from  $u$  to any  $u_{ID}$  has weight not greater than  $1/|ID| + \Delta$ , i.e.  $W_{max}(u, u_{ID}) \leq 1/|ID| + \Delta$ ;

2. does not know anything about  $ID$  (particular elements or size), the path from  $u$  to  $u_{ID}$  has weight not greater than  $\Delta$ , i.e.  $W_{max}(u, u_{ID}) \leq \Delta$ .

There are several proposals for formal frameworks for anonymity [8, 9] and unlinkability [16]. Frameworks introduced in these papers define typed systems with several defined categories like agents, type of agents, messages [9] or an inductive system based on modal logic of knowledge [8]. We believe that our proposal would be more flexible and would cover context information as an inherent part of the model thus opening interesting questions.



**Figure 6. En example with a PATS model graph.**

**The example:** Let us express our example from part 1.4 in the PATS model. Figure 6 shows how the context information about typical basket contents is connected to actual instances of shoppings. As we are interested in connections between payment cards (pseudonyms), we are looking for paths (and their aggregate values) containing pairs of particular payment cards. Let us try to find paths between card 11 and the other two cards:

Path	Probabilities	Aggregate
11 – A – l – B – 21	$1 * 0.9 * 0.1 * 1$	0.09
11 – A – l – C – 25	$1 * 0.9 * 0.8 * 1$	0.72
11 – A – m – B – 21	$1 * 0.1 * 0.9 * 1$	0.09
11 – A – m – C – 25	$1 * 0.1 * 0.2 * 1$	0.02
...	...	...

**Figure 7. Paths connecting payment card 11 with the other two cards**

These are the shortest (and highest value) paths only. The attacker may deduce (with a high probability) that payment cards 11 and 25 belong to the same person, though she does not know who this person is. According to our definitions, unlinkable pseudonymity is breached.

## 6. Conclusions and open issues

This paper points out that contexts provide (or perhaps we can even say that they produce) side-channels that are not covered neither by the Common Criteria Privacy Class, nor by the Freiburg Privacy Diamond model. We also believe that contexts in general are not well reflected in other current research attempts to quantify the levels (and deterioration) of privacy. A simplistic introduction of pseudonyms will not guarantee perfect privacy, and we need to have some means to quantify what levels of privacy is needed and/or achievable for specific scenarios. There are two solutions for protection against side-channels: hiding and so-called anonymizing. Hiding is what anonymizing networks utilise – they combine number of messages together, thus creating satisfactory anonymity set. Anonymizing (or rather more often in practice pseudonymising) requires creation of layers that cloak the identity of the protected entity. Common Criteria use this concept when defining pseudonymity that still enforces accountability of users, but hides/shades their identity.

One particularly interesting issue relates to the Common Criteria definition of unlinkability, as empirically reviewed by Rannenberg and Iachello [13, 14] and more formally specified above in section 2.4, is whether the unlinkable “items” in question should only be operations (service invocations) or whether other kinds of unlinkability should also be considered. We have provided a supporting evidence for a substantial revision of unlinkability specifications, while leaving the actual revision as an item for the future research.

We also provide our basic PATS model that is not so limited in the coverage of selected aspects of user interactions and therefore allows for better quantification/measurement of different aspects of privacy. This proposal, unlike the CC or FPD models, introduces a computational model (based on graph theory). One of the problems we are currently examining is atomicity for the vertices, i.e. contextual information. We currently review various approaches to this problem, being aware that the issue of atomicity has a critical impact on the possibility of graph normalisation and therefore also for the provision of the critical properties of completeness and soundness. This work in progress includes the issue of edge dependence, for it is clear that the edges are not completely independent. We can mark sets of nodes from distinct kinds of context (e.g., pseudonyms, IP addresses used in connections from the same provider) – let us call them *domains*. Then we can address additional graph properties, e.g., such that for all pairs of domains  $D_1, D_2$ , all sums of probabilities from any node in  $D_1$  to all nodes in  $D_2$  are not higher than a given value, typically 1.

The PATS approach allows for two definitions of anonymity, a weaker one considering a weight of the entire path from  $u_{ID}$  to  $s_i$  can be added to the stronger one

above that considers the intermediate edges from  $u_{ID}$  only (to any other vertex – contextual information – that would then be identifiable).

Another interesting issue is the role of time that has a two-fold role – firstly, it can be a contextual information (time of an action invoked by a certain subject, i.e. three mutually connected vertices). Secondly, the probabilistic weights of edges in a graph change with time, as do the sets of vertices and edges as such. Obviously, the contextual role of time may be reflected by the latter view – time of an action invoked by a certain subject is denoted by existence of vertices describing action and subject identifiers, connected by an edge with weight 1, at the given time.

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